

Inference at * 2 2 1 2 1 1 1 1
of proof for Lemma p-fun-exp-add-sq:

....subterm.... T:t1:n

1. $A : \text{Type}$
 2. $f : A \rightarrow (A + \text{Top})$
 3. $x : A$
 4. $m : \mathbb{Z}$
 5. $0 < m$
 6. $\forall n:\mathbb{N}. (\uparrow\text{can-apply}(f^{\wedge} m - 1; x)) \Rightarrow ((f^{\wedge} n + (m - 1)(x)) \sim (f^{\wedge} n(\text{do-apply}(f^{\wedge} m - 1; x))))$
 7. $n : \mathbb{N}$
 8. $\uparrow\text{can-apply}(f^{\wedge} m; x)$
 9. $\neg(n = 0)$
 10. $\neg(n + m = 0)$
 11. $\neg(n = 0)$
 12. $\neg(m = 0)$
 13. $\uparrow\text{can-apply}(f^{\wedge} m - 1; x)$
 14. $x_1 : A$
 15. $\text{do-apply}(f^{\wedge} m - 1; x) = x_1$
- $\vdash f(x_1) = f^{\wedge} m(x)$
by ((Unfold 'p-fun-exp' (0)·)
CollapseTHEN ((RecUnfold 'primrec' 0)
CollapseTHEN ((
(if (0) =0 then SplitOnConclITE else SplitOnHypITE (0))·)
CollapseTHEN (Auto·)·

CollapseTHEN (((Try (Trivial))·)
CollapseTHEN ((Reduce 0)
CollapseTHEN (
Fold 'p-fun-exp' 0)·)·)·)·)
CollapseTHEN (((if (first_bool F:b
) then HypSubst' else RevHypSubst') (-2)(0))·)
CollapseTHEN (Auto·)·
- 1:

16. $\neg(m = 0)$
 $\vdash f(\text{do-apply}(f^{\wedge} m - 1; x)) = f \circ f^{\wedge} m - 1 (x)$
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